

AMC 8 1998
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1 For $x = 7$, which of the following is the smallest?

- (A) $\frac{6}{x}$ (B) $\frac{6}{x+1}$ (C) $\frac{6}{x-1}$ (D) $\frac{x}{6}$ (E) $\frac{x+1}{6}$

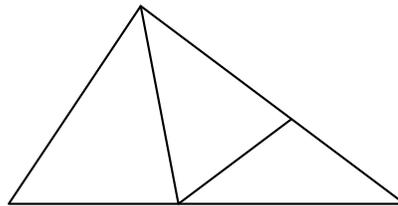
2 If $\frac{a}{c} \mid \frac{b}{d} = a \cdot d - b \cdot c$, what is the value of $\frac{3}{1} \mid \frac{4}{2}$

- (A) -2 (B) -1 (C) 0 (D) 1 (E) 2

3 $\frac{\frac{3}{8} + \frac{7}{8}}{\frac{4}{5}} =$

- (A) 1 (B) $\frac{25}{16}$ (C) 2 (D) $\frac{43}{20}$ (E) $\frac{47}{16}$

4 How many triangles are in this figure? (Some triangles may overlap other triangles.)

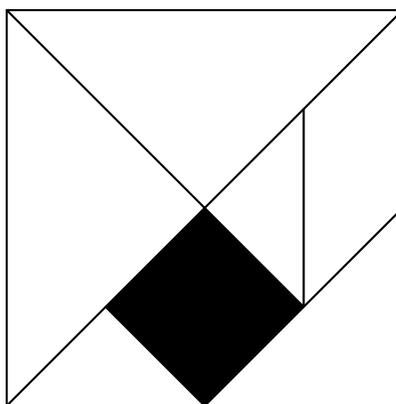


- (A) 9 (B) 8 (C) 7 (D) 6 (E) 5

5 Which of the following numbers is largest?

- (A) 9.12344 (B) $9.123\overline{4}$ (C) $9.12\overline{34}$ (D) $9.1\overline{234}$ (E) $9.\overline{1234}$

6 Dots are spaced one unit apart, horizontally and vertically. The number of square units enclosed by the polygon is



- (A) $\frac{1}{6}$ (B) $\frac{1}{7}$ (C) $\frac{1}{8}$ (D) $\frac{1}{12}$ (E) $\frac{1}{16}$

- 14** An Annville Junior High School, 30% of the students in the Math Club are in the Science Club, and 80% of the students in the Science Club are in the Math Club. There are 15 students in the Science Club. How many students are in the Math Club?

- (A) 12 (B) 15 (C) 30 (D) 36 (E) 40

- 15** Problems 15, 16, and 17 all refer to the following:
In the very center of the Irenic Sea lie the beautiful Nisos Isles. In 1998 the number of people on these islands is only 200, but the population triples every 25 years. Queen Irene has decreed that there must be at least 1.5 square miles for every person living in the Isles. The total area of the Nisos Isles is 24,900 square miles.

15. Estimate the population of Nisos in the year 2050.

- (A) 600 (B) 800 (C) 1000 (D) 2000 (E) 3000

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16. Estimate the year in which the population of Nisos will be approximately 6,000.

- (A) 2050 (B) 2075 (C) 2100 (D) 2125 (E) 2150

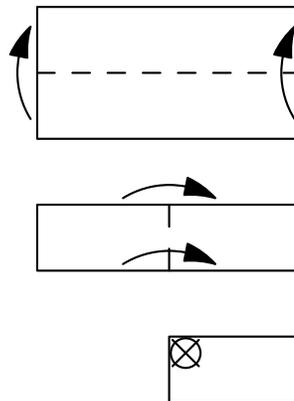
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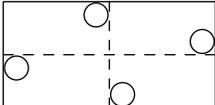
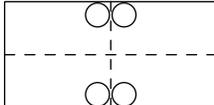
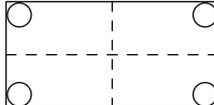
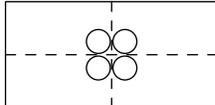
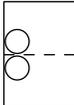
that there must be at least 1.5 square miles for every person living in the Isles. The total area of the Nisos Isles is 24,900 square miles.

17. In how many years, approximately, from 1998 will the population of Nisos be as much as Queen Irene has proclaimed that the islands can support?

- (A) 50 yrs. (B) 75 yrs. (C) 100 yrs. (D) 125 yrs. (E) 150 yrs.

18. As indicated by the diagram below, a rectangular piece of paper is folded bottom to top, then left to right, and finally, a hole is punched at X. What does the paper look like when unfolded?

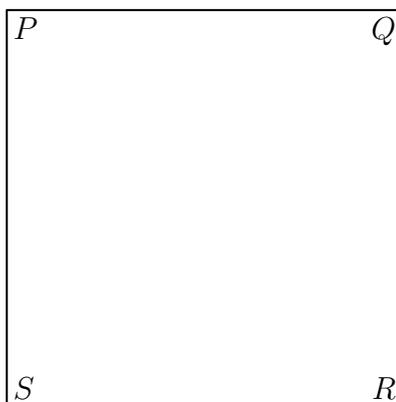


- (A)  (B)  (C)  (D)  

19. Tamika selects two different numbers at random from the set $\{8, 9, 10\}$ and adds them. Carlos takes two different numbers at random from the set $\{3, 5, 6\}$ and multiplies them. What is the probability that Tamika's result is greater than Carlos' result?

- (A) $\frac{4}{9}$ (B) $\frac{5}{9}$ (C) $\frac{1}{2}$ (D) $\frac{1}{3}$ (E) $\frac{2}{3}$

20. Let $PQRS$ be a square piece of paper. P is folded onto R and then Q is folded onto S . The area of the resulting figure is 9 square inches. Find the perimeter of square $PQRS$.



- (A) 9 (B) 16 (C) 18 (D) 24 (E) 36

21 A $4 * 4 * 4$ cubical box contains 64 identical small cubes that exactly fill the box. How many of these small cubes touch a side or the bottom of the box?

- (A) 48 (B) 52 (C) 60 (D) 64 (E) 80

22 Terri produces a sequence of positive integers by following three rules. She starts with a positive integer, then applies the appropriate rule to the result, and continues in this fashion.

Rule 1: If the integer is less than 10, multiply it by 9.

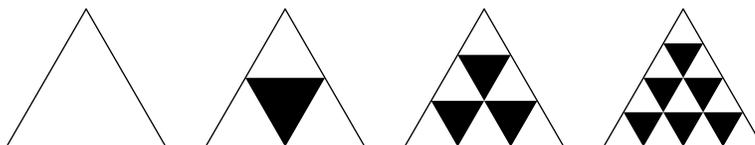
Rule 2: If the integer is even and greater than 9, divide it by 2.

Rule 3: If the integer is odd and greater than 9, subtract 5 from it.

Find the 98th term of the sequence that begins 98, 49,

- (A) 6 (B) 11 (C) 22 (D) 27 (E) 54

23 If the pattern in the diagram continues, what fraction of the interior would be shaded in the eighth triangle?



- (A) $\frac{3}{8}$ (B) $\frac{5}{27}$ (C) $\frac{7}{16}$ (D) $\frac{9}{16}$ (E) $\frac{11}{45}$

24 A rectangular board of 8 columns has squared numbered beginning in the upper left corner and moving left to right so row one is numbered 1 through 8, row two is 9 through 16, and so on. A

