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by parmenides51

- 1 268 numbers are written around a circle. The 17th number is 3, the 83rd is 4 and the 144th is 9. The sum of every 20 consecutive numbers is 72. Find the 210th number.

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- 2  $A, B, C$  can walk at 5 km/hr. They have a car that can accommodate any two of them which travels at 50 km/hr. Can they reach a point 62 km away in less than 3 hrs?

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- 3  $C$  is the circle center  $(0, 1)$ , radius 1.  $P$  is the parabola  $y = ax^2$ . They meet at  $(0, 0)$ . For what values of  $a$  do they meet at another point or points?

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- 4 For which integers  $n \geq 8$  is  $n^{\frac{1}{n-7}}$  an integer?

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- 5 The reals  $a, b$  satisfy
$$\begin{cases} a^3 - 3a^2 + 5a - 17 = 0 \\ b^3 - 3b^2 + 5b + 11 = 0. \end{cases}$$
Find  $a + b$ .

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- 6 A tetrahedron has five edges of length 3 and circumradius 2. What is the length of the sixth edge?

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