

## **AoPS Community**

www.artofproblemsolving.com/community/c2014653 by jasperE3

**Problem 1** Given non-zero real numbers u, v, w, x, y, z, how many different possibilities are there for the signs of these numbers if

$$(u+ix)(v+iy)(w+iz) = i?$$

**Problem 2** If a convex set of points in the line has at least two diameters, say AB and CD, prove that AB and CD have a common point.

Problem 3 Assume that the numbers from the table

satisfy the inequality:

$$\sum_{j=1}^{n} |a_{j1}x_1 + a_{j2}x_2 + \ldots + a_{jn}x_n| \le M,$$

for each choice  $x_i = \pm 1$ . Prove that

 $|a_{11} + a_{22} + \ldots + a_{nn}| \le M.$ 

**Problem 4** Determine the largest integer k(n) with the following properties: There exist k(n) different subsets of a given set with n elements such that each two of them have a non-empty intersection.

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1

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