

AoPS Community

2015 Mediterranean Mathematical Olympiad

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- Let $P(x) = x^4 x^3 3x^2 x + 1$. Prove that there are infinitely many positive integers *n* such 1 that $P(3^n)$ is not a prime.
- 2 Prove that for each triangle, there exists a vertex, such that with the two sides starting from that vertex and

each cevian starting from that vertex, is possible to construct a triangle.

In the Cartesian plane \mathbb{R}^2 , each triangle contains a Mediterranean point on its sides or in its 3 interior, even if the triangle is degenerated into a segment or a point. The Mediterranean points have the following properties: (i) If a triangle is symmetric with respect to a line which passes through the origin (0,0), then the Mediterranean point lies on this line.

(ii) If the triangle *DEF* contains the triangle *ABC* and if the triangle *ABC* contains the Mediterranean points M of DEF, then M is the Mediterranean point of the triangle ABC.

Find all possible positions for the Mediterranean point of the triangle with vertices (-3, 5), (12, 5), (3, 11).

In a mathematical contest, some of the competitors are friends and friendship is mutual. Prove 4 that there is a subset M of the competitors such that each element of M has at most three friends in M and such that each competitor who is not in M, has at least four friends in M.

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