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by parmenides51

- 1 Four right triangles, each with the sides 1 and 2, are assembled to a figure as shown. How large a fraction does the area of the small circle make up of that of the big one?
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- 2 Prove that for any integer n there exist integers a, b and c such that $n = a^2 + b^2 - c^2$.

- 3 Can 29 boys and 31 girls be lined up holding hands so no one is holding hands with two girls?

- 4 It is stated that 2^{2010} is a 606-digit number that begins with 1. How many of the numbers $1, 2, 2^2, 2^3, \dots, 2^{2009}$ start with 4?

- 5 An equilateral triangle ABC is given. With BC as diameter, a semicircle is drawn outside the triangle. On the semicircle, points D and E are chosen such that the arc lengths BD, DE and EC are equal. Prove that the line segments AD and AE divide the side BC into three equal parts.
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