

## **AoPS Community**

## Kosovo Team Selection Test 2016

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1	Solve equation in real numbers
	$\sqrt{x + \sqrt{4x + \sqrt{16x + \sqrt{+\sqrt{4^n x + 3}}}}} - \sqrt{x} = 1$
2	Show that for all positive integers $n \ge 2$ the last digit of the number $2^{2^n} + 1$ is 7.
3	If quadratic equations $x^2 + ax + b = 0$ and $x^2 + px + q = 0$ share one similar root then find quadratic equation for which has roots of other roots of both quadratic equations .
4	It is given the function $f : \mathbb{R} \to \mathbb{R}$ fow which $f(1) = 1$ and for all $x \in \mathbb{R}$ satisfied
	$f(x+5) \ge f(x) + 5$ and $f(x+1) \le f(x) + 1$
	If $g(x) = f(x) - x + 1$ then find $g(2016)$ .
5	Let be ABC an acute triangle with $ AB  >  AC $ Let be D point in side AB such that $ ACD  =$

**5** Let be ABC an acute triangle with |AB| > |AC|. Let be D point in side AB such that  $\angle ACD = \angle CBD$ . Let be E the midpoint of segment BD and S let be the circumcenter of triangle BCD. Show that points A, E, S and C lie on a circle.

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