## AoPS Community

## Kosovo Team Selection Test 2016

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1 Solve equation in real numbers

$$
\sqrt{x+\sqrt{4 x+\sqrt{16 x+\sqrt{+\sqrt{4^{n} x+3}}}}}-\sqrt{x}=1
$$

2 Show that for all positive integers $n \geq 2$ the last digit of the number $2^{2^{n}}+1$ is 7 .
3 If quadratic equations $x^{2}+a x+b=0$ and $x^{2}+p x+q=0$ share one similar root then find quadratic equation for which has roots of other roots of both quadratic equations .
$4 \quad$ It is given the function $f: \mathbb{R} \rightarrow \mathbb{R}$ fow which $f(1)=1$ and for all $x \in \mathbb{R}$ satisfied
$f(x+5) \geq f(x)+5$ and $f(x+1) \leq f(x)+1$
If $g(x)=f(x)-x+1$ then find $g(2016)$.
$5 \quad$ Let be $A B C$ an acute triangle with $|A B|>|A C|$. Let be $D$ point in side $A B$ such that $\angle A C D=$ $\angle C B D$. Let be $E$ the midpoint of segment $B D$ and $S$ let be the circumcenter of triangle $B C D$ . Show that points $A, E, S$ and $C$ lie on a circle .

