## AoPS Community

## Balkan MO 1994

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$1 \quad$ An acute angle $X A Y$ and a point $P$ inside the angle are given. Construct (using a ruler and a compass) a line that passes through $P$ and intersects the rays $A X$ and $A Y$ at $B$ and $C$ such that the area of the triangle $A B C$ equals $A P^{2}$.

Greece
2 Let $n$ be an integer. Prove that the polynomial $f(x)$ has at most one zero, where

$$
f(x)=x^{4}-1994 x^{3}+(1993+n) x^{2}-11 x+n .
$$

Greece
3 Let $a_{1}, a_{2}, \ldots, a_{n}$ be a permutation of the numbers $1,2, \ldots, n$, with $n \geq 2$. Determine the largest possible value of the sum

$$
S(n)=\left|a_{2}-a_{1}\right|+\left|a_{3}-a_{2}\right|+\cdots+\left|a_{n}-a_{n-1}\right| .
$$

Romania
4 Find the smallest number $n \geq 5$ for which there can exist a set of $n$ people, such that any two people who are acquainted have no common acquaintances, and any two people who are not acquainted have exactly two common acquaintances.

## Bulgaria

