## AoPS Community

## Balkan MO 1998

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1 Consider the finite sequence $\left\lfloor\frac{k^{2}}{1998}\right\rfloor$, for $k=1,2, \ldots, 1997$. How many distinct terms are there in this sequence?

Greece
2 Let $n \geq 2$ be an integer, and let $0<a_{1}<a_{2}<\cdots<a_{2 n+1}$ be real numbers. Prove the inequality

$$
\sqrt[n]{a_{1}}-\sqrt[n]{a_{2}}+\sqrt[n]{a_{3}}-\cdots+\sqrt[n]{a_{2 n+1}}<\sqrt[n]{a_{1}-a_{2}+a_{3}-\cdots+a_{2 n+1}} .
$$

## Bogdan Enescu, Romania

3 Let $\mathcal{S}$ denote the set of points inside or on the border of a triangle $A B C$, without a fixed point $T$ inside the triangle. Show that $\mathcal{S}$ can be partitioned into disjoint closed segemnts.

Yugoslavia
4 Prove that the following equation has no solution in integer numbers:

$$
x^{2}+4=y^{5} .
$$

Bulgaria

