

AoPS Community

1996 Turkey Junior National Olympiad

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www.artofproblemsolving.com/community/c4156 by xeroxia

- **1** There are 20 balls in a bag. *a* of them are red, *b* of them are white, and *c* of them are black. It is known that
 - if we double the white balls, the probability of drawing one red ball is $\frac{1}{25}$ less than the probability of drawing one red ball at the beginning, and

• if we remove all red balls, the probability of drawing one white ball is $\frac{1}{16}$ more than the probability of drawing one white ball at the beginning.

Find a, b, c.

2 Write out the positive integers consisting of only 1s, 6s, and 9s in ascending order as in: $1, 6, 9, 11, 16, \ldots$

a. Find the order of 1996 in the sequence.

b. Find the 1996th term in the sequence.

3 Let *P* be a point inside of equilateral $\triangle ABC$ such that $m(\widehat{APB}) = 150^{\circ}$, $|AP| = 2\sqrt{3}$, and |BP| = 2. Find |PC|.

