## AoPS Community

## Turkey Junior National Olympiad 1996

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1 There are 20 balls in a bag. $a$ of them are red, $b$ of them are white, and $c$ of them are black. It is known that

- if we double the white balls, the probability of drawing one red ball is $\frac{1}{25}$ less than the probability of drawing one red ball at the beginning,
and
- if we remove all red balls, the probability of drawing one white ball is $\frac{1}{16}$ more than the probability of drawing one white ball at the beginning.

Find $a, b, c$.
2 Write out the positive integers consisting of only $1 \mathrm{~s}, 6 \mathrm{~s}$, and 9 s in ascending order as in: $1,6,9,11,16, \ldots$.
a. Find the order of 1996 in the sequence.
b. Find the 1996th term in the sequence.

3 Let $P$ be a point inside of equilateral $\triangle A B C$ such that $m(\widehat{A P B})=150^{\circ},|A P|=2 \sqrt{3}$, and $|B P|=2$. Find $|P C|$.

