

**Turkey Junior National Olympiad 2004**

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by xeroxia

- 1 Let  $[AD]$  and  $[CE]$  be internal angle bisectors of  $\triangle ABC$  such that  $D$  is on  $[BC]$  and  $E$  is on  $[AB]$ . Let  $K$  and  $M$  be the feet of perpendiculars from  $B$  to the lines  $AD$  and  $CE$ , respectively. If  $|BK| = |BM|$ , show that  $\triangle ABC$  is isosceles.

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- 2 The positive integer  $n$  is the sum of two positive integers that divide  $n + 6$ . Find all possible values of  $n$ .

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- 3 On the evening, more than  $\frac{1}{3}$  of the students of a school are going to the cinema. On the same evening, More than  $\frac{3}{10}$  are going to the theatre, and more than  $\frac{4}{11}$  are going to the concert. At least how many students are there in this school?

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