

AoPS Community

2014 Nordic

Nordic 2014

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- **1** Find all functions $f : N \to N$ (where N is the set of the natural numbers and is assumed to contain 0), such that $f(x^2) f(y^2) = f(x+y)f(x-y)$ for all $x, y \in N$ with $x \ge y$.
- **2** Given an equilateral triangle, find all points inside the triangle such that the distance from the point to one of the sides is equal to the geometric mean of the distances from the point to the other two sides of the triangle.
- **3** Find all nonnegative integers *a*, *b*, *c* such that

$$\sqrt{a} + \sqrt{b} + \sqrt{c} = \sqrt{2014}.$$

A game is played on an $n \times n$ chessboard. At the beginning there are 99 stones on each square. Two players A and B take turns, where in each turn the player chooses either a row or a column and removes one stone from each square in the chosen row or column. They are only allowed to choose a row or a column, if it has least one stone on each square. The first player who cannot move, looses the game. Player A takes the first turn. Determine all n for which player A has a winning strategy.

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