

AoPS Community

1999 Spain Mathematical Olympiad

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www.artofproblemsolving.com/community/c691162 by parmenides51

-	Day 1
1	The lines t and t', tangent to the parabola $y = x^2$ at points A and B respectively, intersect at point C. The median of triangle ABC from C has length m. Find the area of $\triangle ABC$ in terms of m.
2	Prove that there exists a sequence of positive integers $a_1, a_2, a_3,$ such that $a_1^2 + a_2^2 + + a_n^2$ is a perfect square for all positive integers n .
3	A one player game is played on the triangular board shown on the picture. A token is placed on each circle. Each token is white on one side and black on the other. Initially, the token at one vertex of the triangle has the black side up, while the others have the white sides up. A move consists of removing a token with the black side up and turning over the adjacent tokens (two tokens are adjacent if they are joined by a segment). Is it possible to remove all the tokens by a sequence of moves?
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- 4 5	png Day 2 A box contains 900 cards, labeled from 100 to 999. Cards are removed one at a time without replacement. What is the smallest number of cards that must be removed to guarantee that the

the same point. What is the smallest number of lines needed so that N > 1999?

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