

Bangladesh Mathematical Olympiad 2018

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1 Solve:

$$x^2(2-x)^2 = 1 + 2(1-x)^2$$

Where x is real number.

2 BdMO National 2018 Higher Secondary P2

AB is a diameter of a circle and AD & BC are two tangents of that circle. AC & BD intersect on a point of the circle. $AD = a$ & $BC = b$. If $a \neq b$ then $AB = ?$

3 BdMO National 2018 Higher Secondary P3

Nazia rolls four fair six-sided dice. She doesn't see the results. Her friend Faria tells her that the product of the numbers is 144. Faria also says the sum of the dice, S satisfies $14 \leq S \leq 18$. Nazia tells Faria that S cannot be one of the numbers in the set $\{14, 15, 16, 17, 18\}$ if the product is 144. Which number in the range $\{14, 15, 16, 17, 18\}$ is an impossible value for S ?

4 Yukihira is counting the minimum number of lines m , that can be drawn on the plane so that they intersect in exactly 200 distinct points. What is m ?

5 Four circles are drawn with the sides of quadrilateral $ABCD$ as diameters. The two circles passing through A meet again at E . The two circles passing through B meet again at F . The two circles passing through C meet again at G . The two circles passing through D meet again at H . Suppose, E, F, G, H are all distinct. Is the quadrilateral $EFGH$ similar to $ABCD$? Show with proof.

6 Find all the pairs of integers (m, n) satisfying the equality $3(m^2 + n^2) - 7(m + n) = -4$

7 Evaluate

$$\int_0^{\pi/2} \frac{\cos^4 x + \sin x \cos^3 x + \sin^2 x \cos^2 x + \sin^3 x \cos x}{\sin^4 x + \cos^4 x + 2 \sin x \cos^3 x + 2 \sin^2 x \cos^2 x + 2 \sin^3 x \cos x} dx$$

8 a tournament is playing between n persons. Everybody plays with everybody one time. There is no draw here. A number k is called n good if there is any tournament such that in that tournament they have any player in the tournament that has lost all of k 's.

prove that

1. n is greater than or equal to $2^{k+1} - 1$

2. Find all n such that 2 is a n -good