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– Grade XI

1 Solve the equation,

$$\sqrt{x+5} + \sqrt{16-x^2} = x^2 - 25$$

2 Sides of a triangle form an arithmetic sequence with common difference 2, and its area is 6 cm^2 . Find its sides.

3 In a right $\triangle ABC$ ($\angle C = 90^\circ$), CD is the height. Let r_1 and r_2 be the radii of inscribed circles of $\triangle ACD$ and $\triangle DCB$. Find the radius of inscribed circle of $\triangle ABC$

4 Solve the equation,

$$\sin(\pi \log x) + \cos(\pi \log x) = 1$$

5 Prove that if the angles α and β satisfy $\sin(\alpha + \beta) = 2 \sin \alpha$,
Then

$$\alpha < \beta$$
